

1 Complete the table below, to find the angle between the stated vectors.

Points	Angle	Diagram	Vectors	Magnitudes	Scalar Product	Angle Calculation
$A(5, 3, 2)$ $B(6, -1, 5)$ $C(-1, 7, 10)$	$\angle ABC$		$\vec{BA} = \begin{pmatrix} 5 \\ 3 \\ 2 \end{pmatrix} - \begin{pmatrix} 6 \\ -1 \\ 5 \end{pmatrix} = \begin{pmatrix} -1 \\ 4 \\ -3 \end{pmatrix}$ $\vec{BC} = \begin{pmatrix} -1 \\ 7 \\ 10 \end{pmatrix} - \begin{pmatrix} 6 \\ -1 \\ 5 \end{pmatrix} = \begin{pmatrix} -7 \\ 8 \\ 5 \end{pmatrix}$	$ \vec{BA}  = \sqrt{(-1)^2 + 4^2 + (-3)^2}$ $ \vec{BA}  = \sqrt{26}$  $ \vec{BC}  = \sqrt{(-7)^2 + 8^2 + 5^2}$ $ \vec{BC}  = \sqrt{138}$	$\vec{BA} \cdot \vec{BC} = (-1 \times -7) + (4 \times 8) + (-3 \times 5)$ $\vec{BA} \cdot \vec{BC} = 24$	$\cos \theta = \frac{\vec{BA} \cdot \vec{BC}}{ \vec{BA}   \vec{BC} }$ $\cos \theta = \frac{24}{\sqrt{26}\sqrt{138}}$ $\theta = \cos^{-1} \frac{24}{\sqrt{26}\sqrt{138}}$ $\theta = 66.38^\circ$
$O(0,0,0)$ $A(6,4,2)$ $C(2, 4, 6)$	$\angle AOC$					
$A(5, 3, 2)$ $B(6, -1, 5)$ $C(-1, 7, 10)$	$\angle BCA$					
$A(2, -1, 3)$ $B(3, 6, 5)$ $C(6, 6, -2)$	$\angle BAC$					
$A(5, 3, 2)$ $B(6, -1, 5)$ $C(-1, 7, 10)$	$\angle ABC$					